## Exponents Study Guide

Math 1
Name: $\qquad$
Date: $\qquad$ Block: $\qquad$
Directions: Simplify each expression. Use positive exponents.

1. $\left(\frac{y^{5}}{x^{4}}\right)^{-3}$
2. $\frac{p^{3} q^{-1}}{q^{2} r^{-6}}$
3. $\left(\frac{16 x^{-4}}{32 y^{-5}}\right)^{2}$
4. $\left(m^{3} n^{-5} m^{-1}\right)^{-3}$
5. $\left(\frac{3^{2} y^{-4}}{3^{2} x^{0} y^{2}}\right)^{2}$

$$
\left(\frac{x^{4} y^{-2}}{x^{-3} y^{5}}\right)^{-1}
$$

6. If $z=1 / 2$, which expression has the greatest value?
a) $z^{-6} z^{4}$
b) $\left(z^{-2} z^{5}\right)^{-2}$
c) $\left(z^{3}\right)^{5}$
d) $-\left(z^{2} z^{-4}\right)^{-3}$

Simplify the following:
7. $\left(\frac{9 a^{-3}}{18 b^{-4}}\right)^{2}$
8. $\left(\frac{5^{3} t^{-2}}{5^{3} s^{0} t^{3}}\right)^{2}$
9. $\left(x^{-2}\right)^{-5}$
10. $\left(x^{2} y^{-2}\right)(x y)^{4}$

Write using rational exponents.
11. $(\sqrt[3]{3 a})^{4}$
12. $\frac{1}{(\sqrt{3 k})^{5}}$
13. $(\sqrt[3]{6 x})^{4}$
14. $(\sqrt[4]{m})^{3}$

Write using radicals.
15. $(10 n)^{\frac{3}{2}}$
16. $\left(27 p^{6}\right)^{\frac{5}{3}}$
17. $(5 x)^{-\frac{5}{4}}$
18. $a^{\frac{6}{5}}$

Graph each function. Make sure to draw a dotted line for the horizontal asymptote.
19. $f(x)=\frac{1}{3} \cdot 3^{x}-2$
20. $y=3 \cdot\left(\frac{1}{3}\right)^{x}+2$
21. $y=0.5^{x}+3$


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a. How much will the Honda be worth in 2012?
b. How much will the Ford be worth in 2015?
23. The function $y=195 \cdot 0.75^{x}$ models the average time (in minutes) of math tests in 1980.
a. Does the exponential function represent growth or decay?
b. Estimate the average time for math tests in 1990.
c. Predict the average time for math tests in 2025.
24. Find the balance in a bank account after 8 years if $\$ 500$ is invested at $7 \%$ interest.
25. Find the balance in a bank account after 5 years if $\$ 2000$ is invested at $6 \%$ interest.
26. On the first swing, a pendulum swings through an arc of length 60 cm . On each successive swing, the length of the arc is $82 \%$ of the length of the previous swing.
a. Write a rule to model this situation.
b. Find the length of the arc on the fifth swing. Round your answer to the nearest cm .
27. Reasoning: Does the table below represent an exponential function? Explain why or why not.

| $x$ | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: |
| $y$ | 2.25 | 3.375 | 5.063 | 7.953 |

28. 

Bacteria in a culture are growing exponentially with time, as shown in the table below.

## Bacteria Growth

| Day | Bacteria |
| :---: | :---: |
| 0 | 100 |
| 1 | 200 |
| 2 | 400 |

Which of the following equations expresses the number of bacteria, $y$, present at any time, $t$ ?
a) $y=100+2^{t}$
*b) $y=(100) \cdot(2)^{t}$
c) $y=2^{t}$
d) $y=(200) \cdot(2)^{t}$
29. This table shows the number of subscribers to four magazines.

| Year | Subscribers to <br> Music Magazine | Subscribers to <br> Sports Magazine | Subscribers to <br> Business Magazine | Subscribers to <br> History Magazine |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 100,000 | 100,000 | 100,000 | 100,000 |
| 2 | 90,000 | 90,000 | 90,000 | 90,000 |
| 3 | 81,000 | 80,000 | 70,000 | 85,000 |
| 4 | 72,900 | 70,000 | 40,000 | 82,500 |

Which magazine's subscribers are best modeled by an exponential function?

