## Properties: Zero and Negative Exponents

| Zero as an Exponent | For every nonzero number $a$, <br> $a^{0}=1$ | Examples: |
| :---: | :---: | :---: |
| Negative Exponent | For every nonzero number $a$ and integer $n$, <br> $a^{-1}=\frac{1}{a^{n}}$ | Examples: |

## Zero Base and Zero Exponents

Why can't you use 0 as a base and an exponent? Solve each of the following. $3^{0}=\quad 2^{0}=\quad 1^{0}=\quad 0^{0}=$

However, consider the following pattern.
$0^{3}=$
$0^{2}=$
$0^{1}=$
$0^{0}=$

It is not possible for $0^{0}$ to equal both 1 and 0 . Therefore, $0^{0}$ is $\qquad$ -.

## Simplifying Powers

What is the simplified form of each expression?
a) $9^{-2}=$
b) $3.6^{0}=$

Got it? What is the simplified form of each expression?
a) $4^{-3}=$
b) $(-5)^{0}=$
C) $3^{-2}=$
d) $6^{-1}=$
e) $(-4)^{-2}=$

## Simplifying Exponential Expressions

What is the simplified form of each expression?
a) $5 a^{3} b^{-2}$
b) $\frac{1}{x^{-5}}=$

Got it? What is the simplified form of each expression?
a) $x^{-9}=$
b) $\frac{1}{n^{-3}}=$
C) $4 c^{-3} b=$
d) $\frac{2}{a^{-3}}=$
e) $\frac{n^{-5}}{m^{2}}=$

## Evaluating an Exponential Expression

What is the value of $3 s^{3} t^{-2}$ for $s=2$ and $t=-3$ ?

Got it? What is the simplified form of each expression if $n=-2$ and $w=5$ ?
a) $n^{-4} w^{0}$
b) $\frac{n^{-1}}{w^{2}}$
C) $\frac{n^{0}}{w^{6}}$
d) $\frac{1}{n w^{-1}}$

| Dividing Powers with the Same Base |  |  |
| :--- | :--- | :--- |
| To divide powers with the same base, <br> subtract the exponents. | $\frac{a^{m}}{a^{n}}=$ | $\frac{x^{4}}{x^{7}}=$ |

Why it Works: Use repeated multiplication to rewrite the product of powers: $38 \div 3^{6}=$ ?

1. Expand each into the product numbers to the right.

$$
\frac{3^{8}}{3^{6}}=(\square)=
$$

## Dividing Algebraic Expressions

What is each expression written using each base only once?
a) $\frac{4 x^{8}}{2 x^{3}}=$
b) $\frac{9 m^{2} n^{4}}{-12 m^{5} n^{3}}=$
c) $\frac{-9 k^{6} j^{2}}{36 k j^{5}}=$
d) $\frac{5^{-2} a^{-3} b^{7}}{2 a^{5} b^{2}}=$

| Raising a Quotient to a Power |  |  |
| :--- | :--- | :--- |
| To raise a quotient to a power, raise <br> the numerator and the denominator <br> to the power and simplify. | $\left(\frac{a}{b}\right)^{n}=$ | $\left(\frac{3}{5}\right)^{3}=$ |

Why it Works: Use repeated multiplication to rewrite the product of powers: $\left(\frac{x}{y}\right)^{3}$

1. Expand each into the product numbers to the right.

$$
\left(\frac{x}{y}\right)^{3}=\square=\square=
$$

## Raising a Quotient to a Power

a) What is the simplified form of $\left(\frac{z^{4}}{5}\right)^{3}$ ?
b) What is the simplified form of $\left(\frac{4}{x^{3}}\right)^{2}$ ?

| Raising a Quotient to a Negative Power |  |  |
| :---: | :---: | :---: |
| To raise a quotient to a negative <br> power, raise the numerator and the <br> denominator to the power and <br> simplify. | $\left(\frac{a}{b}\right)^{-n}=$ | $\left(\frac{h}{g}\right)^{-3}=$ |

## Simplifying an Exponential Expression

a) What is the simplified form of $\left(\frac{2 x^{6}}{y^{4}}\right)^{-3}$ ?
b) What is the simplified form of $\left(\frac{a}{5 b}\right)^{-2}$ ?

